IAT_EX Assignment 1

May 17, 2011

\documentclass[letterpaper,12pt]{article}, \begin{document}, and \end{document}.

Also, within the preample of your document include the command

\usepackage[top=2.5cm, bottom=2.5cm, left=2cm, right=2cm]{geometry}

Reproduce each of the following within your .tex file (you need only reproduce items 1 - 4, including numbering, but not the surrounding directions and hints):

- 1. The derivative of the indirect function f[g(x)] is $\{f[g(x)]\}' = f[g(x)]g'(x)$. For the second derivative of the product of f(x) and g(x) one has [f(x)g(x)]'' = f''(x)g(x) + 2f'(x)g'(x) + f(x)g''(x).
- 2. The reduced cubic equation $y^3 + 3py + 2q = 0$ has one real and two complex solutions when $D = q^2 + p^3 > 0$. These are given by Cardan's formula as

$$y_1 = u + v, \ y_2 = -\frac{u+v}{2} + \frac{i}{2}\sqrt{3}(u-v), \ y_3 = -\frac{u+v}{2} - \frac{i}{2}\sqrt{3}(u-v)$$

where

$$u = \sqrt[3]{-q + \sqrt{q^2 + p^3}}, \ v = \sqrt[3]{-q - \sqrt{q^2 + p^3}}$$

3. Each of the measurements $x_1 < x_2 < \cdots < x_r$ occurs p_1, p_2, \ldots, p_r times. The mean value and standard deviation are then

$$x = \frac{1}{n} \sum_{i=1}^{r} p_i x_i, \quad s = \sqrt{\frac{1}{n} \sum_{i=1}^{r} p_i (x_i - x)^2}$$

where $n = p_1 + p_2 + \dots + p_r$.

4. Although this equation looks very complicated, it should not present any great difficulties:

$$\int \frac{\sqrt{(ax+b)^3}}{x} \mathrm{d}x = \frac{2\sqrt{(ax+b)^3}}{3} + 2b\sqrt{ax+b} + b^2 \int \frac{\mathrm{d}x}{x\sqrt{ax+b}}$$

The same applies to $\int_{-1}^{8} (dx/\sqrt[3]{x}) = \frac{3}{2}(8^{2/3} + 1^{2/3}) = 15/2.$

Some hints on these

- 1. Higher derivatives are made with multiple 'symbols: y'', 'yields y'''.
- 2. Use $mathrm{i}$ to denote $\sqrt{-1}$
- 3. Use $\mathbf{d} \in dx$
- 4. Using your favorite online search engine, investigate the $L^{AT}EX$ commands: int, ldots, \cdots, sqrt, and frac
- 5. You may want to try the last one in small chunks of LATEX rather than trying to typeset all at once.