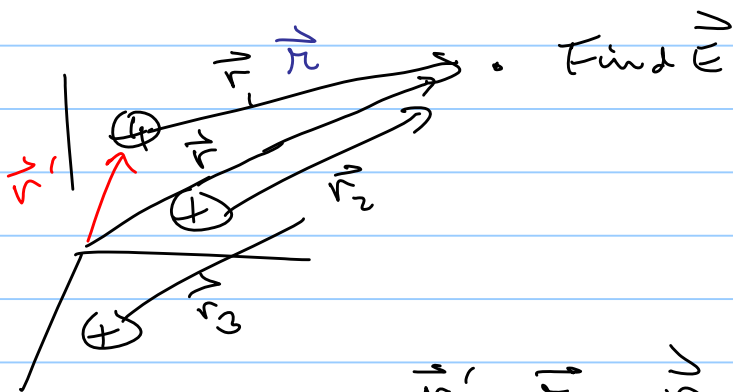


linear

$$F = m a$$

$$F = -k x \quad \text{Spring}$$

$$\omega = \sqrt{\frac{k}{m}}$$



$$\sum \frac{k q_i}{|\vec{r}_i|^2} \hat{r}_i$$

$$\vec{r}' + \vec{r} = \vec{r}$$

↑ locates source pt. ↑ locates field point

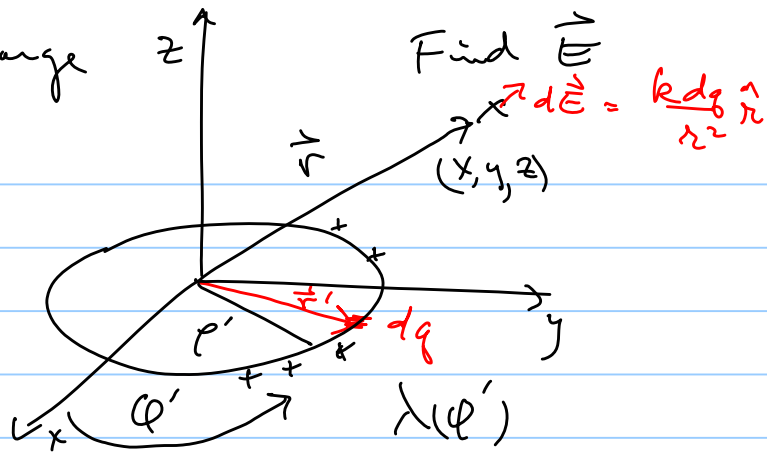
$$\frac{k q_i}{r^2} \hat{r}$$

$$- |\vec{r}| = \left[R \overset{\text{missing}}{\sin \theta'} (\dots \right]$$

Problem: ring of charge

$$\vec{F} = q\vec{E}$$

$$\vec{E} = \int \frac{k dq}{r^2} \hat{r}$$



- find $dq = \lambda dl$ $\int dl = \int_0^{2\pi} \rho d\phi = \rho 2\pi$

$$dq = \lambda(\phi') \rho' d\phi'$$

- find $\vec{r} = \vec{r} - \vec{r}'$

$$\vec{r} = x\hat{x} + y\hat{y} + z\hat{z}$$

$$\vec{r}' = \rho' \hat{\rho}' + \rho' \phi' \hat{\phi}' + z' \hat{z}'$$

$$= \rho \hat{\rho} + \rho \phi' \hat{\phi} + z \hat{z}$$

$$\vec{r}' = \rho' \cos \phi' \hat{x}' + \rho' \sin \phi' \hat{y}' + 0 \hat{z}'$$

$$\sqrt{x'^2 + y'^2} \quad \tan^{-1} \frac{y'}{x'}$$

$$\int d\phi \hat{\phi}$$

↑ not constant as ϕ varies $\hat{\phi}$ so it cannot be taken outside integral

$$\int d\phi \hat{x} \quad \hat{x} \text{ comes outside}$$

$$\vec{r} = \vec{r} - \vec{r}' = (x - \rho' \cos \phi') \hat{x} + (y - \rho' \sin \phi') \hat{y} + (z - 0) \hat{z}$$

$$\hat{r} = \frac{\vec{r}}{|\vec{r}|}$$

$$\vec{E} = \int_0^{2\pi} \frac{k \lambda(\varphi') \rho' d\varphi'}{\left[(x - \rho' \cos \varphi')^2 + (y - \rho' \sin \varphi')^2 + z^2 \right]^{3/2}} \left\{ (x - \rho' \cos \varphi') \hat{x} + (y - \rho' \sin \varphi') \hat{y} + z \hat{z} \right\}$$