

**PHGN361 Exam 1: NAME**

1. (a) Using the integral form of Gauss's Law, **DERIVE** the electric field due to an infinite **CYLINDER** of charge, with radius  $R$  and charge density  $\rho = Ar$  **AND** a constant surface charge density  $\sigma_0$  at  $r = R$ , where  $A$  is a constant. Find the field both inside and outside the cylinder. (b) Prove that your result is consistent with the differential form of Gauss's Law.

Note  $\nabla \cdot \vec{v} = \frac{1}{s} \frac{\partial}{\partial s}(sv_s) + \frac{1}{s} \frac{\partial}{\partial \phi}(v_\phi) + \frac{\partial}{\partial z}v_z$

2. A sphere of radius  $R$  has volume charge density  $\rho = \rho_0 \sin(\theta) \cos(\phi)r/R$ . Write an **INTEGRAL** expression for the electric field on the x-axis a distance  $x_0 > R$  due to this charge distribution.