

Logarithmic Units

Electrical engineers often use a logarithmic unit, the decibel, when they want to discuss signals or spectra with a wide dynamic range (and sometimes even when they don't).

Decibel. The bel (named after Alexander Graham Bell) is a ratio of powers expressed in log units. For example, if one signal carries 10 times less power than another, we say its power is -1 B [$\log(0.1)$] less than the other, or that it is 1 B down from the other. Similarly, if 100 times less power, 2 B down; if 1000 times less power, 3 B down, and so on.

Engineers prefer the decibel to the bel, and the bel is rarely used. A decibel is $1/10$ of a bel, so if one signal carries 10 times less power than another, we say its power is -10 dB less than the other, or that it is 10 dB down. Similarly, if 100 times less power, 20 dB down; if 1000 times less power, 30 dB down, and so on. If a signal carries $1/2$ the power of another, it is 3 dB down; $1/3$ the power, 5 dB down. What if it carries $1/20$ the power? $1/30$? 10 times more power? 2 times more?

dBm. The decibel is a relative unit—a ratio of powers. We may express power quantitatively in decibels, however, provided that we refer the power to a specific value. That value is commonly taken to be 1 mW; power referred to 1 mW is measured in dBm, or decibels with respect to 1 mW. Thus, $1 \text{ mW} \rightarrow 0 \text{ dBm}$, $0.1 \text{ mW} \rightarrow -10 \text{ dBm}$, and so on.

The spectrum analyzer defaults to dBV, or decibels below 1 V. Because the volt is not a unit of power, measuring power in dBV is problematic, and we recommend that you set the spectrum analyzer to dBm as soon as you want to take quantitative data.