

In order to receive full credit, **SHOW ALL YOUR WORK**. Full credit will be given only if all reasoning and work is provided. When applicable, please enclose your final answers in boxes.

1. (10 Points) Given,

$$my'' + ky = 0, \quad y(0) = 1, \quad y'(0) = -1. \quad (1)$$

- (a) Convert the second-order ODE into a system of first order ODE's.
- (b) Using eigenvalues and eigenvectors, solve the corresponding initial value problem.
- (c) Classify the equilibrium point and sketch a possible phase portrait for the system.