E. Kreyszig, Advanced Engineering Mathematics, 8th ed.

<u>Lecture</u>: The Row Reduction Algorithm

Section 7.3, pgs. 287-295

 $\underline{Module}: 02$

Suggested Problem Set: Suggested Problems : $\{1,\,4,\,8,\,16~\}$

August 29, 2008

E. Kreyszig, Advanced Engineering Mathematics, 8^{th} ed.	Section 7.5, pgs. 302-305
<u>Lecture</u> : Solutions of Linear Systems	Module: 02
Suggested Problem Set: Suggested Problems : {Null }	August 29, 2008

Quote of Lectures 2-5

It is not knowledge, but the act of learning, not possession but the act of getting there, which grants the greatest enjoyment.

Carl Friedrich Gauss (1808)

Last time we studied the algebra of matrices. Specifically, we showed that matrix multiplication is defined in such a way that permits us to write down, in a compactified way, a general linear system of equations. We would now like to study how to solve such systems through operations applied to this compact notation. These operations are often called the rules of row reduction and are transcribed directly from algebraic techniques you have been exposed to before. This gives us three rules, which we can apply to linear systems in augmented matrix form. Thought, the application of these three rules does change the augmented matrix it **does not** change the solution to the linear system. The rules of row reduction are:

- 1. Row Interchanged Any two rows of an augmented matrix can have their positions interchanged.
- 2. Row Scaling Any row of an augmented matrix can be multiplied by a non-zero scalar.
- 3. Row Replacement Any row of an augmented matrix can be replaced by itself summed with a scalar multiple of another row.

Applying these three rules we can see by extending concepts from \mathbb{R}^2 that there are three fundamental types of solution sets for a given linear system $\mathbf{Ax} = \mathbf{b}$. They are:

- 1. Unique Solutions : See Exercise 1
- 2. Nonunique Solutions : See Example 1 and Example 2
- 3. No Solutions : See Example 3

In the following pages I have included the graphs associated with the examples and exercises discussed in class. The ordering is:

- 1. Example 1 Top
- 2. Example 1 Side
- 3. Example 2 Side 1
- 4. Example 2 Side 2
- 5. Exercise 1 Side 1
- 6. Exercise 1 Side 2
- 7. Example 3













