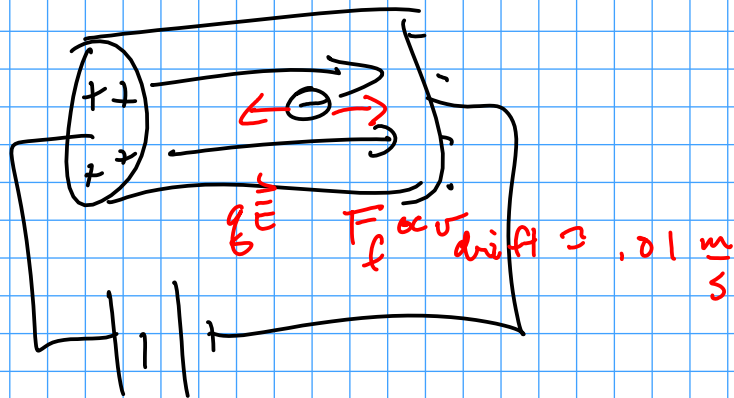


# Ohm's Law



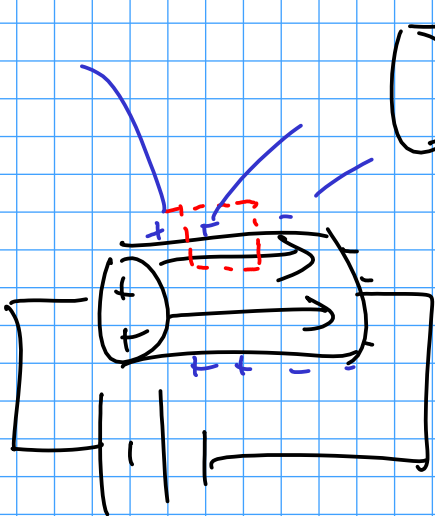
$$v_d \propto E$$

$$\vec{J} = \sigma \vec{E} = \rho \vec{v}$$

Inside conductor

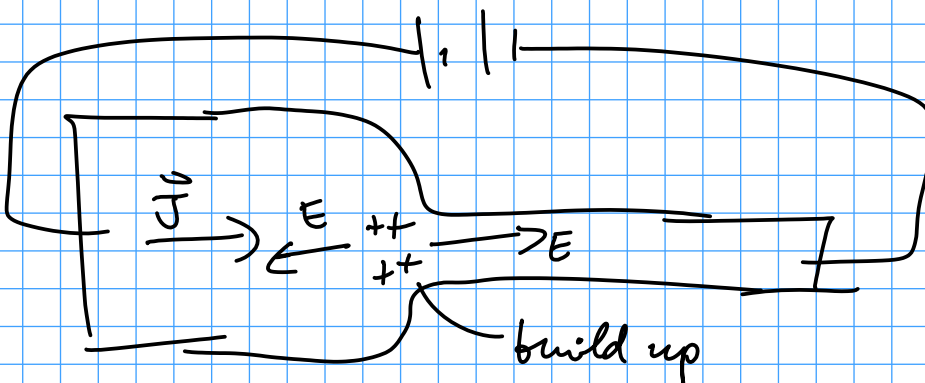
$$\vec{\nabla} \cdot \vec{J} = 0$$

$\vec{J}$  can't flow out  $\Rightarrow E_{\perp} = 0$  in conductor

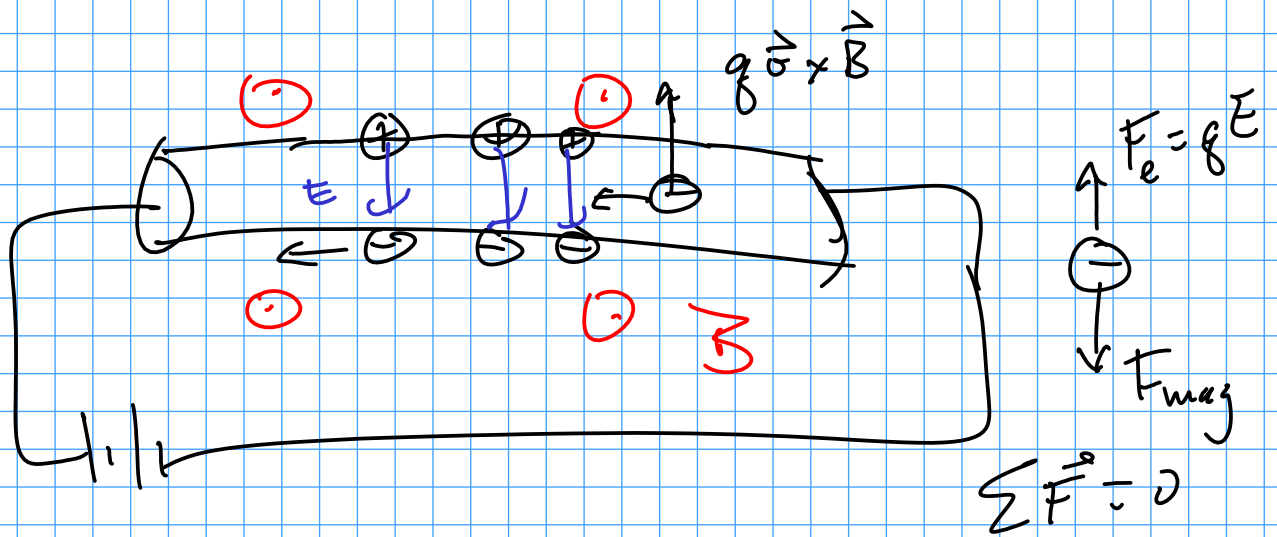


$$\vec{\nabla} \times \vec{E} = 0$$

$$\int_{\partial V} \vec{E} \times \vec{E} \cdot d\vec{a} = \int_V \vec{E} \cdot d\vec{e}$$



$\rho$  const  $\frac{1}{l}$   
flow of an incompressible fluid



$$J = \rho v = -\rho_{\text{elec}} v_{\text{elec}} - \hat{x}$$

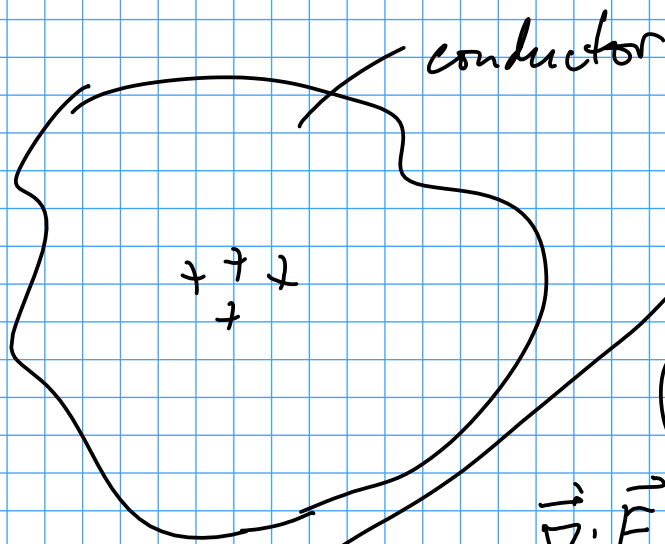
neg

force that moves wire (+ charge of the lattice)

$F_{\text{electric}}$  force from the electrons  
that we moving

$E$  in wire

$$q v B = q E$$



$$\vec{j} = \sigma \vec{E}$$

$$\rho \vec{j} = \sigma \vec{E}$$

Ohm's Law

$$\vec{\nabla} \cdot \vec{E} = \rho / \epsilon_0$$

Gauss's Law  
(Coulombs)

$$\vec{\nabla} \cdot \vec{j} = -\frac{\partial \rho}{\partial t}$$

Cons. charge

$$\vec{\nabla} \cdot \vec{j} = \vec{\nabla} \cdot \sigma \vec{E} = \sigma \underbrace{\vec{\nabla} \cdot \vec{E}}_{\rho / \epsilon_0} = -\frac{\partial \rho}{\partial t}$$

near origin

$$\frac{\sigma}{\epsilon_0} \rho = -\frac{\partial \rho}{\partial t} \Rightarrow \rho = \rho_0 e^{-\frac{\sigma}{\epsilon_0} t}$$

$$\sigma = 10^7 \Omega^{-1} \cdot m \quad \epsilon \text{ in conductor} \Rightarrow \epsilon_0 \approx 10^{-11} \frac{C^2}{N \cdot m^2}$$

