

$$\oint \vec{E} \cdot d\vec{a} = 0 = \frac{Q_{enc}}{\epsilon_0}$$

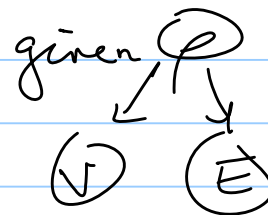
What is the voltage in conductor.

$$\Delta V = - \int_A^B \vec{E} \cdot d\vec{r} = 0 \quad V_B - V_A = 0 \quad V_B = V_A$$

$$V_B - V_C = 0$$

Before

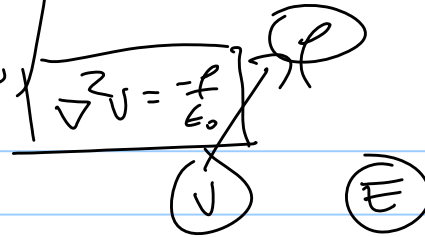
Summation Problem:



$$E = \int \frac{k \rho dr'}{r^2} \hat{r}$$

Boundary Value Problem:

Partial Differential Eqn $\nabla^2 V = -\frac{\rho}{\epsilon_0}$
 boundary condition



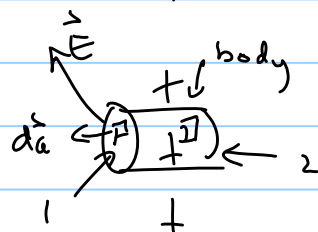
IN vacuum PDE $\rightarrow \nabla^2 V = 0$
 with boundary condition (V is const on boundary)
 region when there is no charge

In class problem

$$\oint \vec{E} \cdot d\vec{a} = \int \vec{E}_1 \cdot d\vec{a} + \int \vec{E}_2 \cdot d\vec{a} + \int \vec{E}_3 \cdot d\vec{a}$$

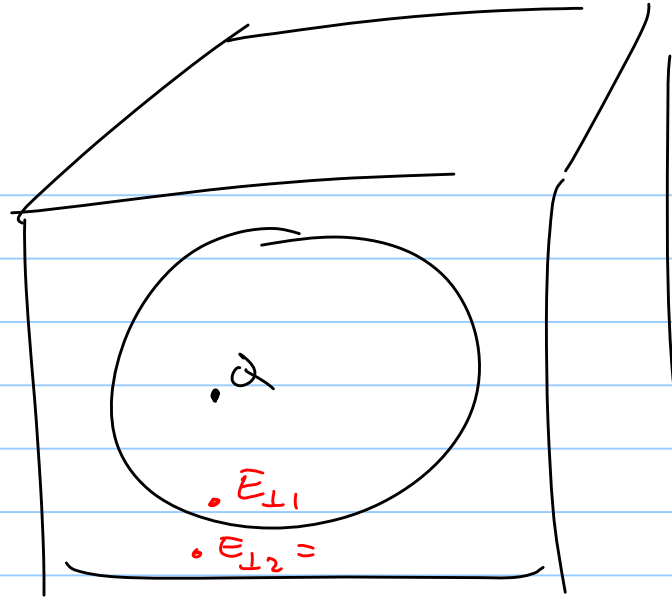
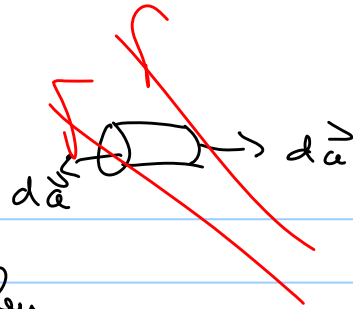
①
②
body

$$EA - EA = \frac{\sigma A}{\epsilon_0} \text{ Crush the can}$$



area end cap is very small but not zero so E is constant over surface

$V(x,y) \approx \text{constant}$ in this region



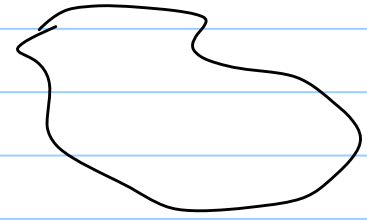
Boundary value problem

find $V(x, y, z)$ in region where there is not charge

Then know $\vec{E} = -\vec{\nabla} V(x, y, z)$

$$E_{\perp 1} - E_{\perp 2} = \frac{\sigma(x, y, z)}{\epsilon_0} \text{ on boundary}$$

Capacitors:



$$\Delta V \propto Q$$

$$\Delta V = \frac{1}{C} Q$$

$$C = \frac{Q}{\Delta V}$$