

## Study guide for Laser Physics in-class midterm.

You may bring in one sheet of paper with anything on it that you want. You should bring a calculator.

### Basic knowledge:

- Converting among  $\lambda$  ,  $\omega$  and  $\nu$  ; converting among widths  $\Delta\lambda$  ,  $\Delta\omega$  and  $\Delta\nu$
- Making simple approximations:  $(1 + \epsilon)^n \approx 1 + n\epsilon$  , small argument  $\sin( )$ ,  $\cos( )$ ,  $\exp( )$ .
- How to calculate intensity, e.g. from energy, beam area and pulse duration

### Interaction of light with atoms

#### Cavity modes and blackbody radiation

- Simple 1-D cavity/resonator: how to derive discrete allowed  $k$ 's,
- Resonance frequencies for a linear cavity, longitudinal mode spacing
- Boltzmann distribution: relative excitation density of two states under thermal

$$\text{equilibrium: } \frac{N_2}{N_1} = \frac{g_2}{g_1} \exp\left(-\frac{E_2 - E_1}{k_B T}\right)$$

#### Einstein A and B coefficients

- Relation of  $B_{12}$  to  $B_{21}$ , and  $A_{21}$  to  $B_{21}$ .
- How to know when spontaneous emission is more likely than emission stimulated by blackbody radiation.
- Constructing and working with simple rate equations that include spontaneous emission, absorption, stimulated emission and external pumping rates (using A, B coeff or using cross-sections). Finding relations under steady-state conditions.

#### Line broadening, line shapes

- Normalized Lorentzian and Doppler (Gaussian) lineshapes.
- Which mechanisms lead to which lineshapes; qualitative difference between homogeneous and inhomogeneous broadening.
- Natural broadening: linkage of exponential damping with Lorentzian lineshape, damping rate with linewidth.
- Decay rate from a single level is the sum of all rates out to destination levels

#### Cross-sections: gain and absorption

- cross-section  $\sigma$  is particular to a given process: the cross-section will depend on initial and final states, as well as whether it is for absorption or stimulated emission.
- The absorption or gain coefficient is  $N\sigma$  , where  $N$  is the number density of the species involved (e.g. inversion density for gain, where  $N = N^*$ ).
- Definition of inversion density

- Exponential behavior of light growth or decay as light propagates in a gain or absorbing medium.
- Role of upper state lifetime as the storage time for gain.
- Calculation of stored, extractable energy (# excited atoms/volume)\*(lasing photon energy).
- Calculation of small signal gain by various methods: inversion density, cross-section and length; stored energy fluence and saturation fluence (both energy/area).
- How spectral dependence of the cross-section affects gain or absorption. For gain, this leads to spectral or spatial gain narrowing.

#### Saturation fluence, saturation intensity

- steady-state (CW) gain:  
small signal, spectrally-dependent gain  $G_0(\omega - \omega_0) = \exp[\alpha(\omega - \omega_0)z]$
- gain coefficient:  $\alpha(\omega - \omega_{21}) = N^* \sigma_{21}(\omega - \omega_{21})$ , where the cross-section includes the appropriate lineshape and broadening
- Saturated gain:  $G(I) = \frac{G_0}{1 + I/I_s}$ ,  $G_0$  and the saturation intensity  $I_s$  in general depend on the frequency difference  $\omega - \omega_{21}$
- Understand that saturation is physically necessary because it is impossible to extract more energy or power from the medium than what it pumped into it.

#### Beam interference

- How to calculate a two-beam interference pattern, starting with the complex expressions for the electric field