Exam schedule: Feb. 7 exam 2 and March 7 exam 3.

Formulas: Memorize Stokes and divergence theorems. Also memorize Gauss's and Ampere's laws along with Biot-Savart for line currents. Memorize forces on surface and volume currents along with the Lorentz force. All calculations involving the divergence and curl will be in cartesian coordinates. However, you should be prepared to apply Ampere's and Gauss's laws in other coordinate systems.

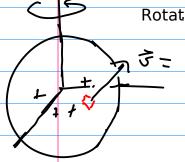
Check out new supplementary material about vector calculus on the wiki.

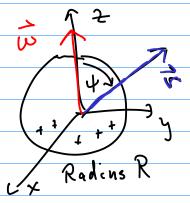
Homework problem:

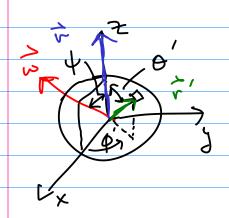
Rotating charged record

Jo = wra

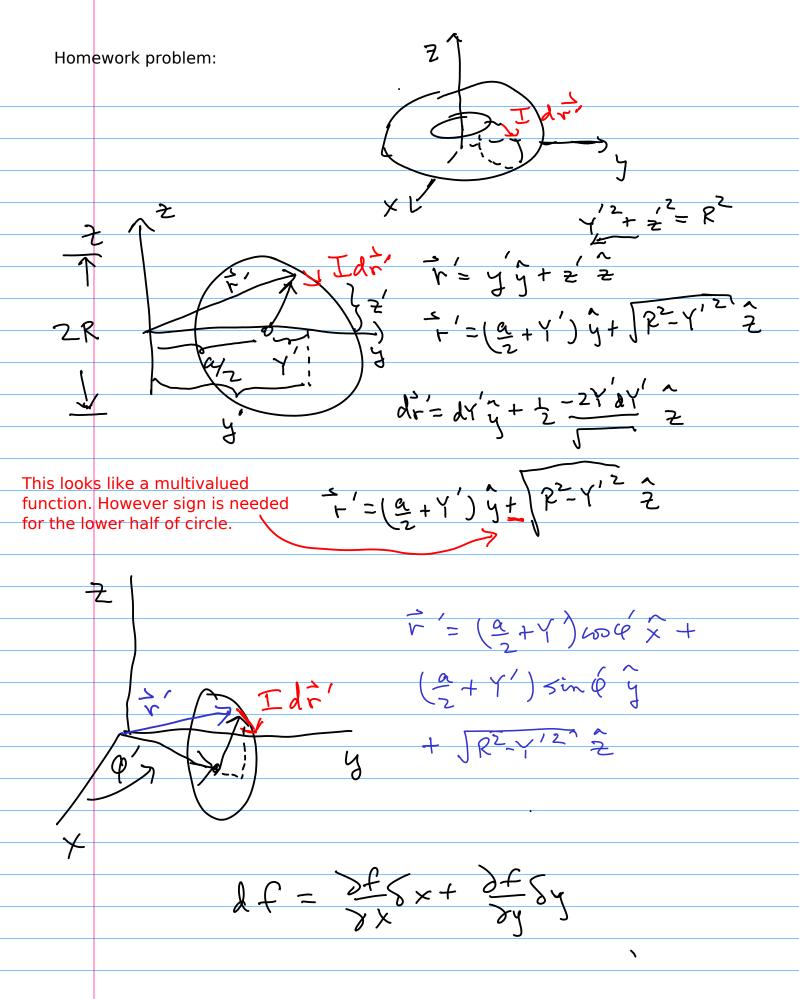
Rotating charged spherical shell







Let is bein the x-z



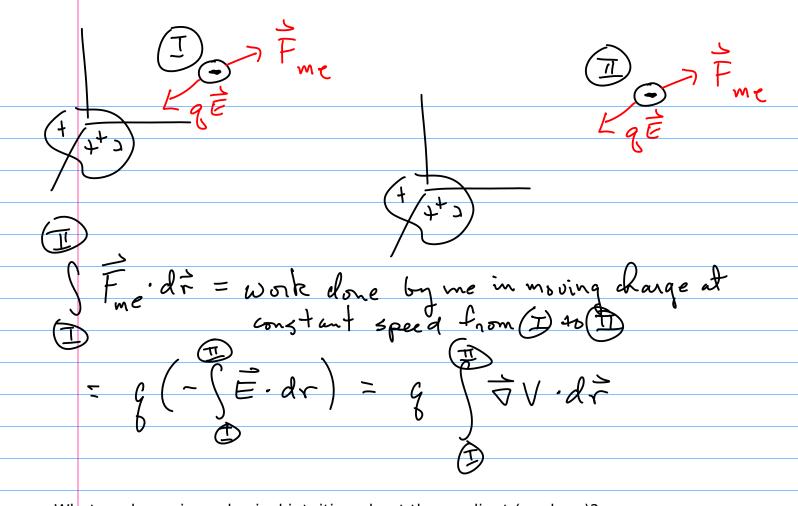
Questions: How do you calculate or show this (congruous)? Just write it out in cartesian coords.

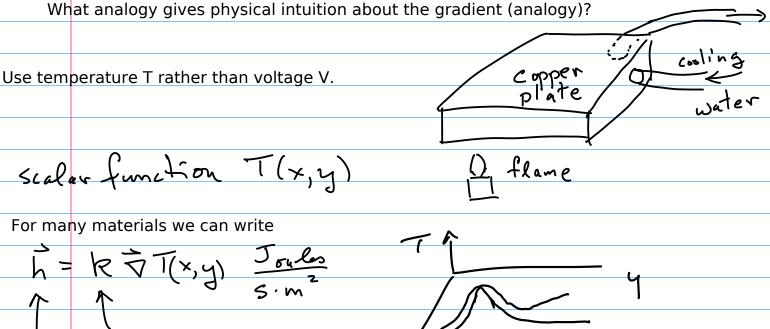
$$\frac{1}{\nabla x} = \frac{1}{2} \frac{1}{2}$$

We can therefore write

Convention

$$-\int \vec{\nabla} \times \vec{\nabla} V \cdot d\vec{a} = \oint \vec{E} \cdot d\vec{r} = 0$$



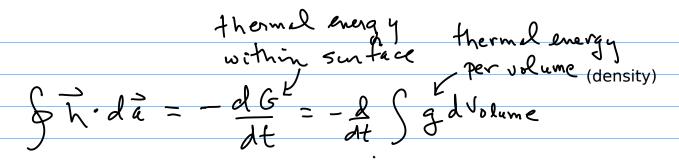


What equation represents heat (energy) flux (informational)?

Thermal conductivity

Called heat flux but what is it (informational)?

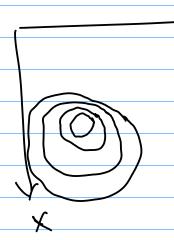
If heat energy is conserved. That is no sources (flames) or sinks (cooling water).



If there is a source or sink

$$\int \vec{h} \cdot d\vec{a} = -\frac{dG}{dt} + \int d\vec{k}$$

What's the differential form using the divergence theorem (congruous)?

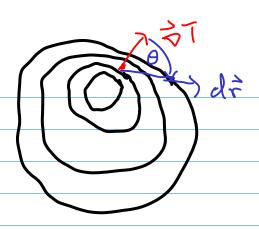


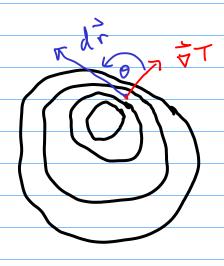
Temperature contour plot

$$\frac{\partial T}{\partial x} = \left[x \frac{\partial T}{\partial x} + \hat{y} \frac{\partial T}{\partial y} + \hat{z} \frac{\partial T}{\partial z}\right] \cdot \left(dx \hat{x} + dy \hat{y} + d\hat{z}\right)$$

$$= \frac{\partial T}{\partial x} dx + \frac{\partial T}{\partial y} dy + \frac{\partial T}{\partial z} dz = \frac{1}{2}$$

Fix the magnitude of dr and change theta.





For what direction of dr is the change in T the greatest (informational)?

dT is greatest when dr moves in direction of grad T

Fundamental theorem of gradients.

$$\frac{1}{2} \cdot d\vec{r} = \left(\hat{x} \frac{\partial T}{\partial x} + \hat{y} \frac{\partial T}{\partial y} + \hat{z} \frac{\partial T}{\partial z}\right) \cdot \left(dx \hat{x} + dy \hat{y} + d\hat{z}\right)$$

$$= \frac{\partial T}{\partial x} dx + \frac{\partial T}{\partial y} dy + \frac{\partial T}{\partial z} dz$$

Differential form
$$\overrightarrow{E} = -\overrightarrow{\nabla} \bigvee$$

Integral form

pt change:
$$V(r) = -\frac{f}{f} \frac{kq}{r^2} dr = k\frac{f}{f}$$

$$\stackrel{\stackrel{\cdot}{=}}{=} \cdot d\hat{r}$$

Superpositon

$$V(r) = \sum_{i} \frac{kg_{i}}{\pi_{i}}$$

