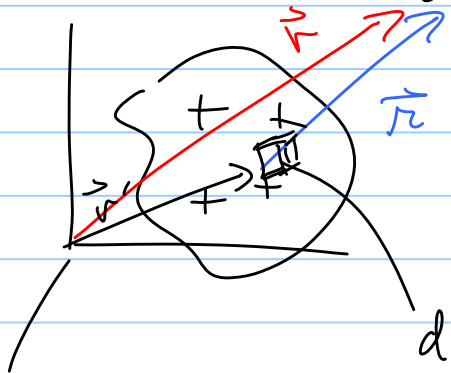


Q find  $\vec{F} = Q \vec{E}$

^ know



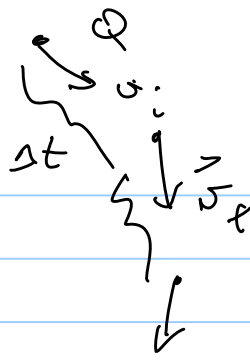
$$\vec{E}(x, y, z) = \int \frac{k \rho(x', y', z') d\tau'}{|\vec{r} - \vec{r}'|^2} \frac{(\vec{r} - \vec{r}')}{|\vec{r} - \vec{r}'|}$$

$$d\tau' = dx' dy' dz'$$

$$\vec{F} = Q \int \frac{k \rho(x', y', z') dx' dy' dz'}{|\vec{r} - \vec{r}'|^2} \frac{(\vec{r} - \vec{r}')}{|\vec{r} - \vec{r}'|} = m \frac{d^2 \vec{r}}{dt^2}$$

$$\vec{F} = m \frac{\Delta \vec{v}}{\Delta t}$$

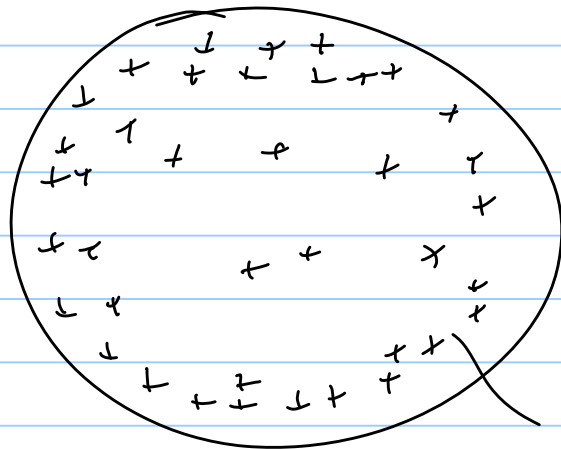
find then solve for  $\Delta \vec{v} = \vec{v}_f - \vec{v}_i$



$$\int \frac{dq}{r^2} = \vec{F} \Delta t$$

$\uparrow$  know       $\uparrow$  integrated to find

Other way to find  $\vec{E}$  is by Gauss's Law



$$\rho = \rho_0 r$$

find  $\vec{E}$  inside the sphere.

Problem solving strat.

- Fundamental princ.

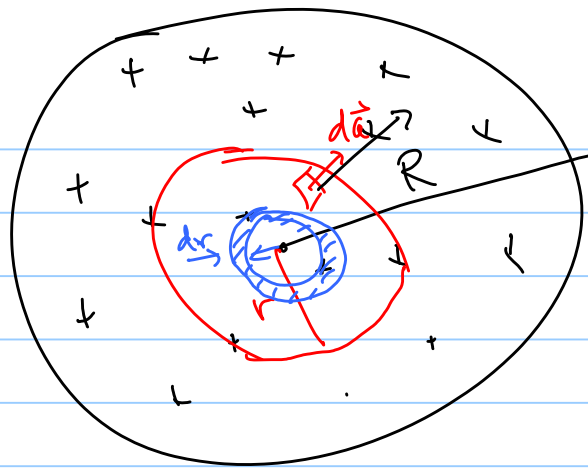
$$\textcircled{1} \vec{E} = \int d\vec{E} = \int \frac{k dq}{r^2} \hat{r}$$

$\textcircled{2}$  Gauss's law

- Outline soln.

- $\textcircled{1}$  find  $dq = \rho dt'$ ,  $\vec{r} = \vec{r} - \vec{r}'$ , limits
- $\textcircled{2}$  use symmetry to find direction of  $\vec{E}$ , then choose Gaussian surface, find  $Q_{\text{enc}}$

- check limits:  $r \rightarrow \infty$  E from pt. charge



$$\oint \vec{E} \cdot d\vec{a} = \frac{Q_{\text{enc}}}{\epsilon_0}$$

$$\vec{E} \cdot d\vec{a} = |\vec{E}| |d\vec{a}| \cos \phi$$

$$\begin{aligned} \oint \vec{E} \cdot d\vec{a} &= \int |\vec{E}| |d\vec{a}| \\ &= E \underbrace{\int |d\vec{a}|}_{4\pi r^2} = E 4\pi r^2 \end{aligned}$$

$$Q_{\text{enc}} = \int \rho(r) d\tau$$

$$d\tau = 4\pi r^2 dr$$

$$\int_0^R 4\pi r^2 dr = \frac{4}{3}\pi R^3$$

$$Q_{\text{enc}} = \int_0^r \rho_0 r' 4\pi r'^2 dr'$$

Gauss's  $E 4\pi r^2 = \frac{Q_{\text{enc}}}{\epsilon_0}$  solve for E