

Table of Common Taylor/Maclaurin Series

$$\begin{aligned}
 \frac{1}{1-t} &= \sum_{n=0}^{\infty} t^n = 1 + t + t^2 + t^3 + \dots \\
 e^t &= \sum_{n=0}^{\infty} \frac{t^n}{n!} = 1 + t + \frac{t^2}{2!} + \frac{t^3}{3!} + \dots \\
 \sin(t) &= \sum_{n=0}^{\infty} \frac{(-1)^n t^{2n+1}}{(2n+1)!} = t - \frac{t^3}{3!} + \frac{t^5}{5!} - \dots \\
 \cos(t) &= \sum_{n=0}^{\infty} \frac{(-1)^n t^{2n}}{(2n)!} = 1 - \frac{t^2}{2!} + \frac{t^4}{4!} - \dots
 \end{aligned}$$

Table of Laplace Transforms

| $f(t)$ | $F(s) = \mathcal{L}\{f(t)\}$ | $f(t)$ | $F(s) = \mathcal{L}\{f(t)\}$ |
|---|---|------------------------------------|------------------------------|
| 1. (a) $f'(t)$ (b) $f''(t)$ | $sF(s) - f(0)$ $s^2F(s) - sf(0) - f'(0)$ | 7. $t^n, n = 1, 2, 3, \dots$ | $\frac{n!}{s^{n+1}}$ |
| 2. $f(t-a)U(t-a)$ $= f(t-a)u_a(t), a \geq 0$ | $e^{-as}F(s)$ | 8. $e^{at}t^n, n = 1, 2, 3, \dots$ | $\frac{n!}{(s-a)^{n+1}}$ |
| 3. $g(t)U(t-a)$ $= g(t)u_a(t), a \geq 0$ | $e^{-as}\mathcal{L}\{g(t+a)\}$ | 9. $\sin(bt)$ | $\frac{b}{s^2+b^2}$ |
| 4. $u_a(t) = U(t-a), a \geq 0$ | $\frac{e^{-as}}{s}$ | 10. $\cos(bt)$ | $\frac{s}{s^2+b^2}$ |
| 5. $\delta_a(t) = \delta(t-a), a \geq 0$ | e^{-as} | 11. $e^{at} \sin(bt)$ | $\frac{b}{(s-a)^2+b^2}$ |
| 6. e^{at} | $\frac{1}{s-a}$ | 12. $e^{at} \cos(bt)$ | $\frac{s-a}{(s-a)^2+b^2}$ |