

MATH-332: Linear Algebra

Chapter: 4

Vector SpacesSection 4.1: Vector Spaces and Subspaces

pgs. 216 - 222

July 13, 2009

Lecture: Vector Spaces and Subspaces**Topics:**

Definition of vector space  
 examples of vector spaces  
 Subspaces w/ examples

**Problems**

Prac: 1, 2  
 Prob: 5-8, 13, 14, 23, 24, 25 - 30 (proofs!)

**Section Goals**

- Understand how the concept of  $\mathbb{R}^n$  can be extended to the concept of a linear vector space and how this mathematical structure can appear in various forms that are critically **not**  $\mathbb{R}^n$ , but do share its algebraic structure.
- Study the concept of a vector subspace and understand how this naturally arises from the definition of spanning sets.

**Section Objectives**

- Define a vector space and show that  $\mathbb{R}^n$  satisfies the definition of a vector space.
- Provide examples of ‘abstract vector spaces.’ That is, show that other mathematical structures share the same algebraic structure of  $\mathbb{R}^n$  and thus are also examples of vector spaces.
- Define a vector subspace and provide examples.
- State theorem 4.1.1 on page 221, which says that given elements of a vector space the set spanned by these vectors forms a vector subspace, and provide a sketch of its proof.