

calculate area of spheres, cylinders
using calculus

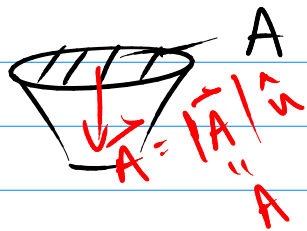
$$\text{Surface area} = \int dA' = \int_0^{2\pi} \int_0^{\pi} R^2 \sin \theta' d\theta' d\phi' = 4\pi R^2$$

Volume element = dV

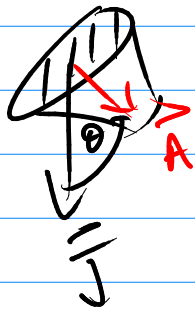
$dV = dr' dA'$

$= r'^2 \sin \theta' d\theta' d\phi' dr'$

$$\text{Volume} = \int dV = \int_0^{\pi} \int_0^{2\pi} \int_0^R r'^2 \sin \theta' d\theta' d\phi' dr' = \frac{4}{3} \pi R^3$$



worm density



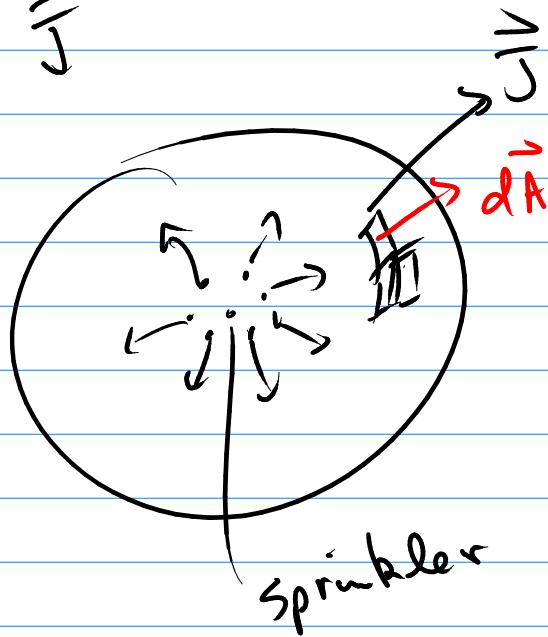
$$\vec{J} \cdot \vec{A} = J A \cos \theta = \Phi$$

↑
flux

$$d\Phi = \vec{J} \cdot d\vec{A}$$

$$= J dA \cos \theta$$

$$\Phi_{\text{spherical surface}} = \int d\Phi = \int \vec{J} \cdot d\vec{A}$$



$$J \propto \frac{1}{r^2}$$

total area of sphere $\propto r^2$

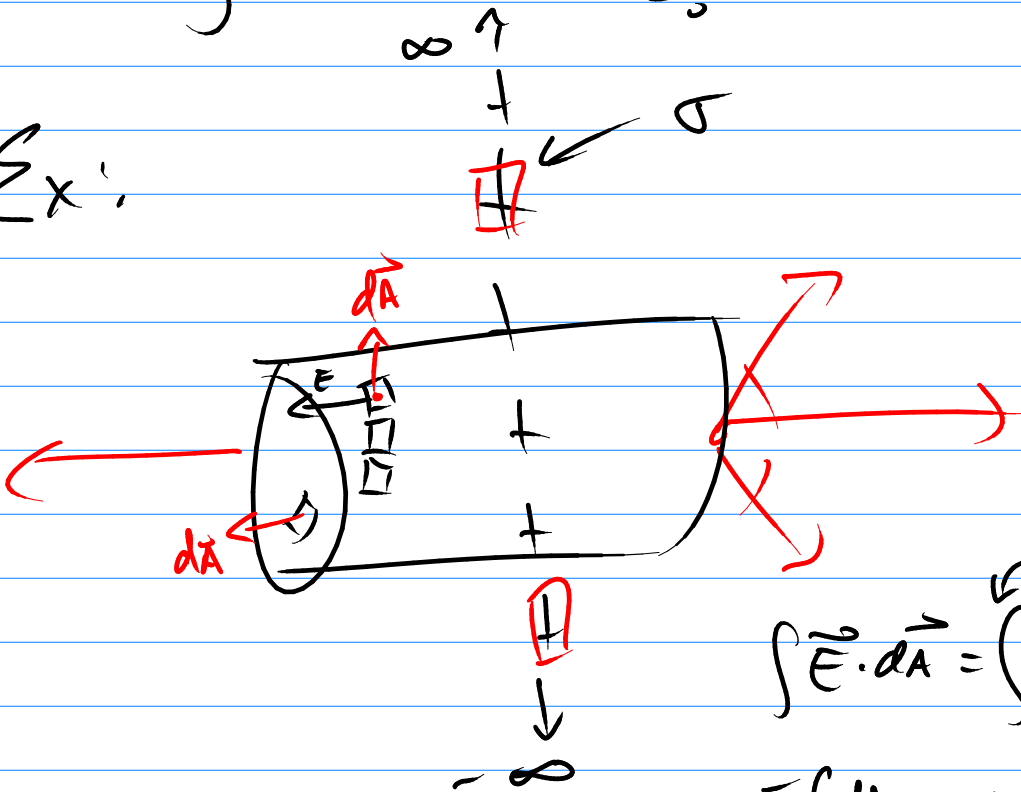
$$\oint \vec{J} \cdot d\vec{a} = \int \frac{\text{particles}}{S}$$

↑
closed surface

Electrostatics $\int \leftrightarrow \vec{E}$
 $\int \leftrightarrow Q$
 particles } Electric field

$$\oint \vec{E} \cdot d\vec{a} = \frac{Q}{\epsilon_0} \quad \text{Gauss's Law}$$

Σ_x :



$$\int \vec{E} \cdot d\vec{A} = \int E dA \cos \phi$$

$$= E \int dA = E \pi R^2$$

$$\oint \vec{E} \cdot d\vec{A} = \int_{\text{cap}} + \int_{\text{cap}} + \int_{\text{body}} = 2E\pi R^2 = \frac{\sigma \pi R^2}{\epsilon_0}$$

$$E = \frac{\sigma}{2\epsilon_0}$$