Homework 3 due 15 Sept. 2006 in class
PH462 EM Waves and Optical Physics posted: 10 Sept 2006

Reading: Heald and Marion (HM) 5.1-5.5, posted notes

1) (from last HW) A beam is polarized in the vertical (y) direction, and propagates in the z-direction. It passes through a half wave plate which can be rotated around the z-axis. Suppose the ordinary axis is at an angle θ to the x-axis.
    a. Express the input state as a linear combination of linearly polarized basis vectors that are aligned with the crystal axes.
    b. Using this representation of the input wave, apply the relative propagation phase shift to the wave that results from the half-wave plate.
    c. Finally, express the output wave in terms of the original basis (the x-y coordinate system) and show that the waveplate rotates linear polarization by 2θ.

2) An *optically active* medium has a refractive index that is different for right- and left-circularly polarized light (n_R and n_L).
    a. Consider an input beam that is initially vertically polarized. It passes through an optically active medium through a distance *d*. Represent the input as a linear combination of R- and L-circular polarized state.
    b. Apply the propagation phase for the two different polarization states to calculate the output polarization state. Show that the output polarization state is always linear, independent of *d*, but with a degree of rotation that linearly depends on *d*.
    c. For crystal quartz, the specific rotation is 21.684 degrees/mm. Calculate the difference between n_R and n_L. Fixed rotators made of quartz are often used in commercial optical systems instead of half-wave plates because they are insensitive to misalignment.

3) HM 5.2

4) HM 5.7

5) HM 5.9. In the first two parts, acounting for all the cosine factors is the main part. For a given ray that is reflected, the direction of the momentum shift of the light is normal to the surface.

6) As an application of the previous problem (part c), calculate the average power of a laser beam required to keep an absorbing sphere of 10^{-8} g and 20μm in diameter floating in midair. Assume the beam is focused to the same diameter as the bead.